

WiSe 2016/17 Semantics 1

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A Semantic Model

1.11.2016

Ambiguity



Readings?

Type of ambiguity?

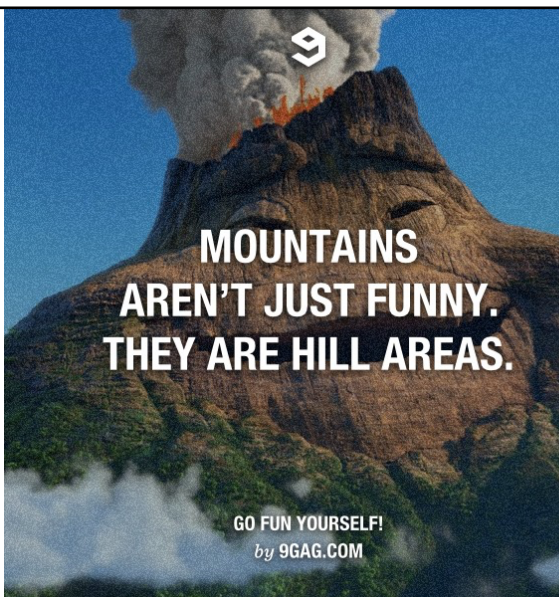
Source of the ambiguity?

*Englischer Rasen
English Lawn*

(found by Eser Abas)

AllDent ~ "al dente"
dentist

Ambiguity



Readings?

Type of ambiguity?


(found by Simon Häfner)

Source of the ambiguity?

Homework

- Work through this wiki page.
- Read Levine et al. (in prep.), Chapter 2, Section 1 [available on olat].
- Define a model and introduce the necessary name symbols and predicate symbols for our scenario with
 - > three individuals
 - > two relations
 - > two properties
- Use your model and your symbols and write down
 - > one formula that is true in your model and
 - > two formulae that are false in your model.

(p. 18: description of spy is not correct!)



$$U = \{ \text{red stick figure}, \text{black stick figure}^E, \text{black stick figure}^v \}$$

 Model $M = \langle U, I \rangle$

 such that


- U is a set of individuals
- I is an interpretation function
- I maps names to individuals
- and predicates to sets of tuples of individuals.

Name symbols

vlad

esha

$I(\text{vlad}) =$ 

$I(\text{osha}) =$ 
The boy has no name!

Names:


$I : \text{Name} \rightarrow U$

I maps names to individuals.

I is a function:

• every name is mapped to 1 ind.

→ no name can refer to more than 1 ind.

→ there can be individuals without name ()

→ every name must refer to an ind.

→ several names can refer to the same individual

$$f(x) = x^2$$

$$f(2) = f(-2) = 4$$

$$I(\text{osk a}) = I(\text{josu}) = \frac{9}{7}$$

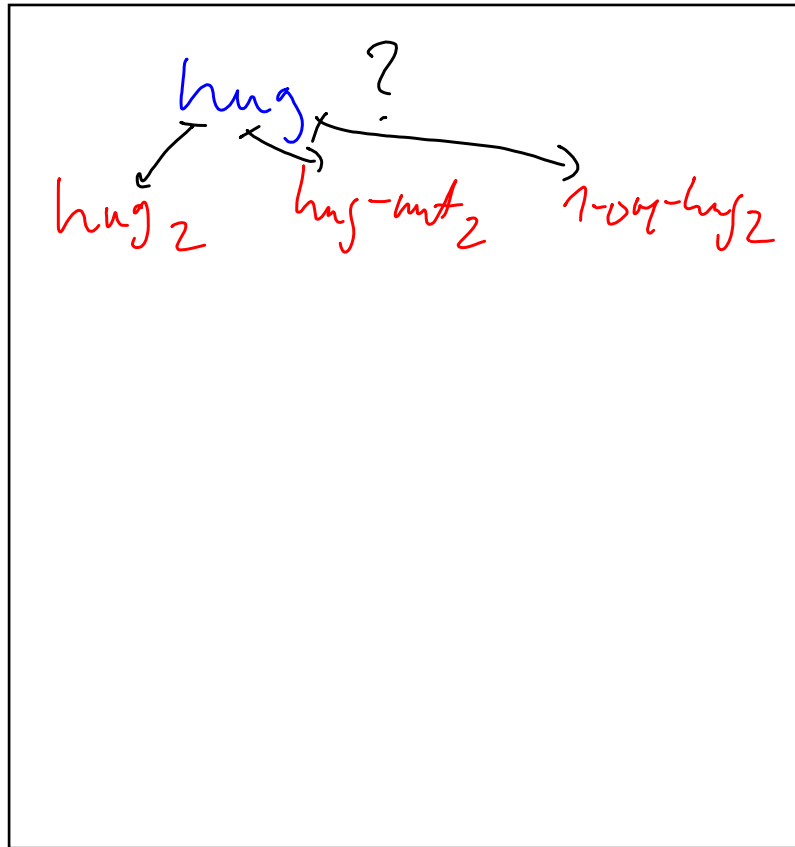
$$I(\text{smaller than } 2)$$

$$= \left\{ \left(\frac{9}{7}, \frac{9}{7} \right), \left(\frac{9}{7}, \frac{9}{7} \right), \left(\frac{9}{7}, \frac{9}{7} \right) \right\}$$

$$= \left\{ (x, y) \mid x \text{ is smaller than } y \right\}$$

Def. by enumeration

Def. by characterization

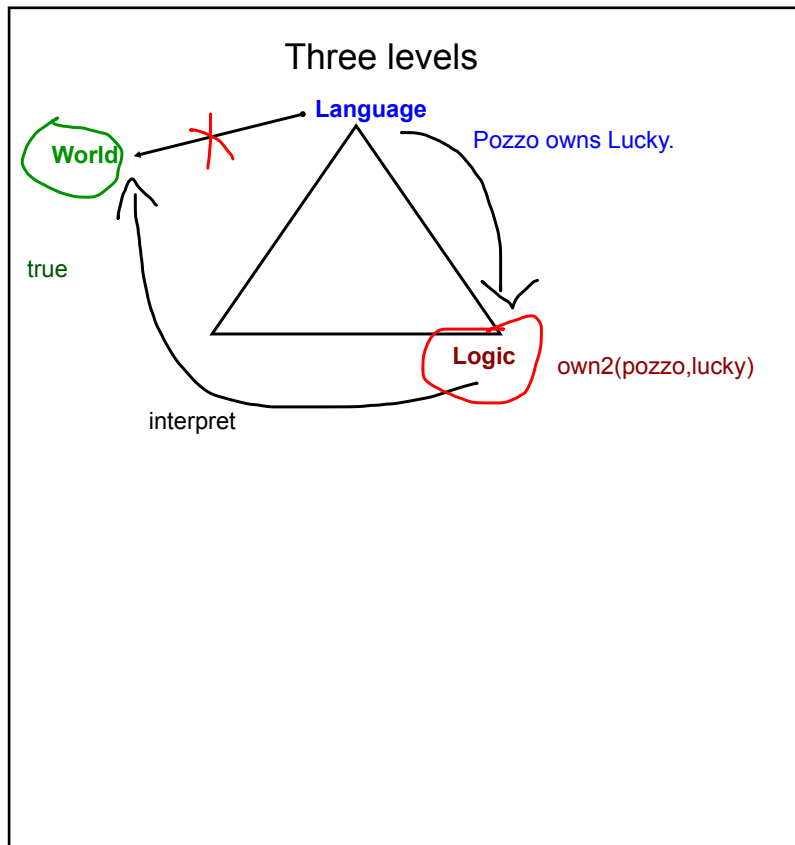
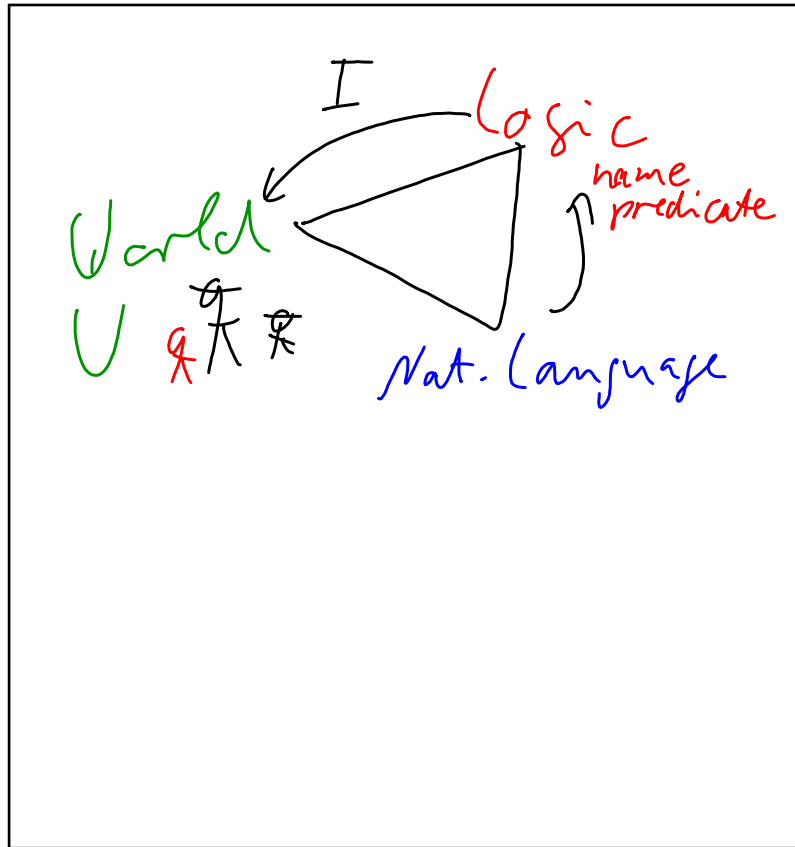


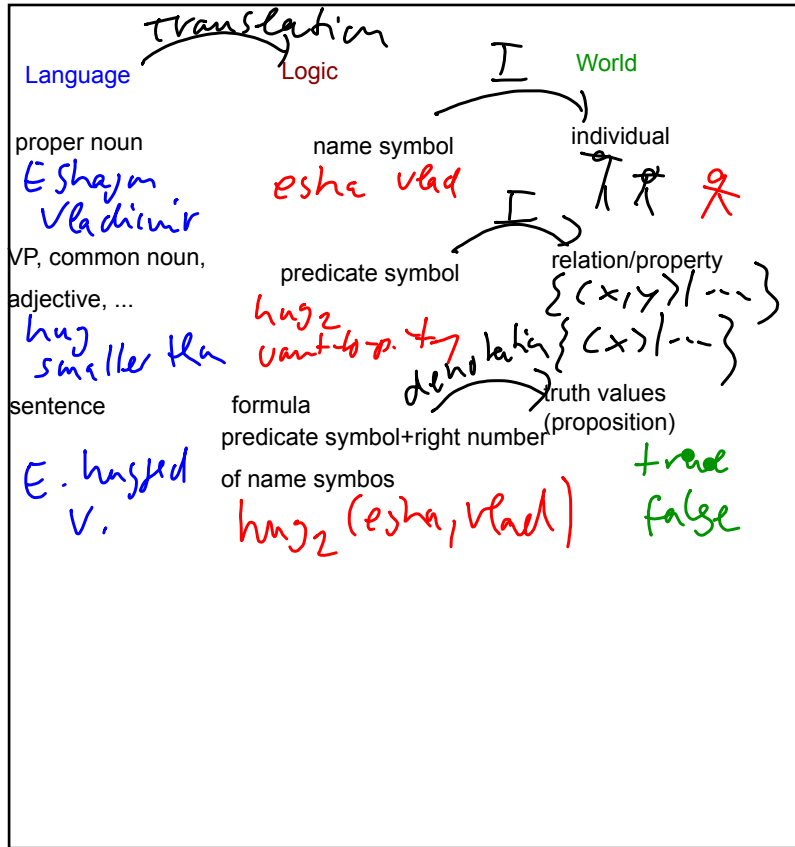
$$\begin{aligned}
 I(hung_2) &= \{ \langle \bar{x}, \bar{y} \rangle, \langle \bar{y}, \bar{x} \rangle \} \\
 &= \{ \langle x, y \rangle \mid x \text{ hangs } y \}
 \end{aligned}$$

$$\begin{aligned}
 I(hung-mutually_2) &= \\
 &= \{ \langle \bar{x}, \bar{y} \rangle, \langle \bar{y}, \bar{x} \rangle \}
 \end{aligned}$$

$$\begin{aligned}
 & I(\text{one-way bus } z) \\
 &= \{ (x, y) \mid x \text{ hangs } y \text{ but} \\
 &\quad y \text{ doesn't hang } x \} \\
 &= \{ \langle \overline{f}, \underline{f} \rangle \}
 \end{aligned}$$

$$\begin{aligned}
 & I(\text{want-to-pass-time } \eta) \\
 &= \{ \langle x \rangle \mid x \text{ wants to pass time} \} \\
 &= \{ \langle \overline{g} \rangle, \langle \underline{g} \rangle \}
 \end{aligned}$$





~~hug₂(vlad, hug₂)~~

Combining expressions to formulae

Syntax: hug₂(esha, vlad)

examples: ~~vlad(esha)~~
hug₂(esha) vlad

general schema:

- predicate symbol
- look at the "number" (arity)
- take that many name symbols
- pred_n(name₁, ..., name_n)

Combining expressions into formulae $\llbracket \dots \rrbracket$

Semantics: $\llbracket \dots \rrbracket$: denotation! $\llbracket \dots \rrbracket$

Formulae are true or false.

$\llbracket \text{smaller-than}_2(\text{vlad}, \text{esha}) \rrbracket$

$\llbracket \text{vlad} \rrbracket = I(\text{vlad})$

$\llbracket \text{smaller-than}_2 \rrbracket = I(\text{smaller-than}_2)$

$\llbracket \text{smaller-than}_2(\text{vlad}, \text{esha}) \rrbracket = \text{true}$

iff ... "truth conditions" ..

$\llbracket \text{smaller-than}_2(\text{vlad}, \text{esha}) \rrbracket = \text{true}$

if and only if (= iff)

$\langle \llbracket \text{vlad} \rrbracket, \llbracket \text{esha} \rrbracket \rangle$ is in $\llbracket \text{smaller-than}_2 \rrbracket$

iff $\langle I(\text{vlad}), I(\text{esha}) \rangle$ is in $I(\text{smaller-than}_2)$

$\mathcal{M} \langle x, y \rangle$ is in $\left\{ \langle x, y \rangle \mid \begin{array}{l} x \text{ is smaller} \\ \text{than } y \end{array} \right\}$

since this is the case,

$\llbracket \text{smaller-than}_2(\text{vlad}, \text{esha}) \rrbracket = \text{true}$

Recipe for atomic formulae

1. Take a predicate symbol.
2. Look at its arity (i.e. the little number subscript)
3. Take the number of name symbols that correspond to the arity.
4. Write down: `predicate-symbol_n(name1, ..., name_n)`

Interpreting formulae: Denotation function

[[...]] depends on the model $M = \langle U, I \rangle$

Denotation of a name:

Denotation of a predicate symbol:

Denotation of an atomic formula:

Computing the truth value of an atomic formula

1. Determine the truth conditions
2. Evaluate them with respect to our model.

Step 1: Determine the truth conditions

$[[\text{homeless1}(\text{estragon})]] = \text{true}$ if and only if (iff)

\mathcal{M}

\mathcal{M}

\mathcal{M}

Step 2: Evaluate them in our model

Since \dots

For next week

- Our literary scenario: see the links in the wiki:
[https://www.lexical-resource-semantics.de/wiki/index.php/Semantics_1,_WiSe_2016/17_\(Sailer\)](https://www.lexical-resource-semantics.de/wiki/index.php/Semantics_1,_WiSe_2016/17_(Sailer))
- Read Levine et al., Chapter 2, Section 2.
- Atomic formulae: Using your model from this week's homework,
 - > Give 2 atomic formulae (one true, one false)
 - > Give 2 statements with 1 connective each. (Use different connectives!)
 - > Provide the step-by-step computation of the truth of your 2 atomic formulae.
- For the computation, watch the videos on the wiki page.
- Find 2 naturally occurring uses of "and" combining two sentences. Is there an extra-meaning in addition to requiring both sentences to be true?

